ORIGINAL ARTICLE

Defnition and validation of a valley amplifcation factor for seismic linear response of 2D homogeneous alluvial basins

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Received: 30 January 2024 / Accepted: 17 July 2024 / Published online: 31 July 2024 © The Author(s) 2024

Abstract

The paper presents fndings from a parametric study analysing geometric (e.g., shape ratio, edge inclination) and stratigraphic factors (e.g. impedance ratio) infuencing ground motion in trapezoidal valleys. The study involved 2160 visco-elastic analyses, considering 180 2D models with diverse shapes and soil properties, undergoing 12 synthetic input motions. Analyses results showed that the motion at the valley centre increases with both shape and impedance ratios, while it is independent of the edge slope; on the other hand, the maximum amplifcation at the edges depends on their inclination and on the impedance ratio, while it is independent of the valley shape. The position and size of the zone of maximum amplifcation at the edges depend on all the previous parameters. A valley amplifcation factor (VAF) is introduced to quantify spectral acceleration increase due to 2D effects. Closed-form equations are proposed to evaluate VAF based on valley properties. The proposed VAF is then applied to predict seismic amplifcation in two central Italian valleys, providing results well-comparable to those obtained from 2D numerical analyses. The described approach can be easily implemented into codes of practice as a conservative design tool to estimate 2D amplifcation along the surface of 'shallow valleys' subjected to moderate seismic actions.

Keywords Seismic site response · 2D valley efects · Valley amplifcation factor · Viscoelastic analysis

1 Introduction

The historical preference for settling in alluvial valleys stems from their strategic proximity to transportation routes and waterways. However, the specifc location of a settlement within the valley signifcantly infuences its vulnerability to natural phenomena like foods,

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landslides, and earthquakes. Macroscopic observations following major earthquakes worldwide (e.g., Loma Prieta, 1989; Northridge, 1994; Kobe, 1995; Athens, 1999; Aterno Valley, 2009; Central Italy, 2016) have consistently revealed a non-uniform distribution of damage in alluvial basins. This phenomenon couldn't be fully explained by stratigraphic efects alone (Pitarka et al. [1996;](#page-38-0) Gao et al. [1996;](#page-37-0) Lanzo et al. [2011](#page-38-1); Chiarini et al. [2011;](#page-37-1) Alleanza et al. [2019a;](#page-36-0) Pagliaroli et al. [2020\)](#page-38-2).

The pioneering analytical studies by Bard and Bouchon [\(1980a](#page-36-1), [b\)](#page-36-2) demonstrated that the intricate interaction among direct, refected, and refracted waves results in ground motion amplifcation that varies signifcantly across the surface of an alluvial basin. This variation depends on the focalization of incoming body waves and the generation of parasitic surface waves. These surface waves can become trapped within the alluvial soil deposit due to the two-dimensional morphology of the valley and the contrast in wave propagation velocities between the bedrock and the flling soil. Consequently, this trapping induces an increase in the amplitude and duration of seismic motion. Subsequent analyses by Bard and Bouchon ([1985\)](#page-36-3), as well as other theoretical studies in applied seismology (e.g., Sanchez-Sesma et al. [1988;](#page-38-3) Bielak et al. [1999;](#page-36-4) Paolucci [1999\)](#page-38-4) and geophysical surveys (e.g., Aki [1988](#page-36-5)) along with weak-motion records by surface arrays (e.g., Faccioli et al. [2002](#page-37-2); De Crescenzo et al. [2018](#page-37-3); Sgattoni et al., [2019](#page-38-5); Sgattoni and Castellaro [2020\)](#page-38-6), confirmed that irregularities may signifcantly modify the amplitude, duration, and frequency content of ground motion.

Despite achieving a satisfactory understanding of the main physical phenomena governing wave propagation in alluvial basins, comprehensively evaluating the quantitative infuence of individual geometrical and mechanical factors remains a challenging issue (Papadimitriou [2019\)](#page-38-7). Consequently, there is no clear and universally accepted methodology for simplifying the estimation of valley efects, unlike the evaluation of topographic effects.

In the literature, several studies have focused on exploring potential updates to seismic codes to incorporate valley efects in conjunction with stratigraphic amplifcation (e.g., Chávez-García and Faccioli [2000](#page-37-4)). Typically, a 'geometric aggravation factor' has been defned as the ratio between results obtained between 2D and 1D analyses, like the approach often adopted by codes of practice to quantify topographic amplifcation (e.g., Bouckovalas and Papadimitriou [2005;](#page-36-6) Pagliaroli et al. [2007](#page-38-8)). Generally, a visco-elastic model is adopted in these analyses, assuming that the geometric aggravation factor is not signifcantly afected by soil non-linearity, which is, however, considered in the stratigraphic amplifcation (see, for instance, Tropeano et al. [2018\)](#page-39-0).

In recent years, numerous parametric studies have been conducted to defne an appropriate valley amplifcation factor (VAF) (e.g., Vessia et al. [2011;](#page-39-1) Riga et al. [2016](#page-38-9); Boudghene-Stambouli et al. [2018;](#page-38-11) Moczo et al. [2018](#page-38-10); Kristek et al. 2018; Zhu et al. [2018a](#page-39-2), [b](#page-39-3), [c;](#page-39-4) Papadimitriou [2019](#page-38-7); Pitilakis et al. [2019](#page-38-12)). However, a solution that adequately considers the infuence of valley geometry and mechanical soil properties on the seismic response to express the variability of VAF along the valley has not been defned yet.

One of the main challenges in formulating a proper valley amplifcation factor is the selection of the 1D reference profle. Two possible approaches are proposed in the literature:

1. *First approach* This assumes as the reference 1D response that computed along the vertical profle corresponding to the center of the valley (e.g., Chávez-García and Faccioli [2000;](#page-37-4) Makra et al. [2005](#page-38-13); Vessia et al. [2011](#page-39-1); Papadimitriou [2019](#page-38-7)). While advantageous

due to reduced computational efort and clear identifcation of the infuence of both geometrical and mechanical parameters on VAF, it may lead to an approximation at the basin edges, where the 1D reference profle can difer signifcantly from that corresponding to the center of the valley. This aspect is less crucial in the case of very shallow trapezoidal valley where most of the valley is characterized by a constant thickness like that at the valley centre.

2. *Second approach* This computes the VAF along the valley profle as the ratio between 2D and 1D site responses, considering the reference 1D profle varying along the valley following the valley shape (e.g., Boudghene-Stambouli et al. [2018](#page-37-5); Moczo et al. [2018;](#page-38-10) Kristek et al. [2018;](#page-38-11) Uzielli et al. [2022\)](#page-39-5). While more accurate, it involves a signifcant computational cost and makes it more challenging to design a simplifed method for evaluating two-dimensional efects.

Following the frst approach, in this study a simple to use visco-elastic Valley Amplifcation Factor is proposed to estimate the 2D amplifcation of homogeneous, symmetrical shallow valleys.

To reach this goal frst an extended parametric study investigating the efects of the main factors afecting the seismic response of shallow valleys (widespread in the territories of Mediterranean countries) was carried out. The results of the numerical analyses performed on regular, simmetrical trapezoidal schemes of homogeneous alluvial valleys, assuming linear visco-elastic behavior, and adopting synthetic input signals with diferent characteristic frequencies, are summarised in Sects. [3](#page-6-0) and [4](#page-10-0). Hence, the VAF has been formulated and the individual infuence of signifcant parameters on VAF has been evaluated and summarised in Sect. [5](#page-22-0) where the limits of the approach are also highlighted. An analytical formulation of the VAF is then proposed that allows quantifying 2D efects on ground motion amplifcation along the entire valley surface, considering basin morphology, the dominant frequency of the input motion, and the mechanical properties of both alluvial soil and bedrock.

Finally, an example of an application to a real valley in Central Italy is presented in Sect. [6,](#page-28-0) comparing the VAFs obtained with complete numerical analyses and with the proposed simplifed ones.

2 Main factors afecting 2D valley seismic response

In the literature, studies on valley effects focus on the role of factors such as:

- (a) Valley shape,
- (b) Rock/soil impedance ratio,
- (c) Bedrock slope at valley edges,
- (d) Soil inhomogeneity,
- (e) Soil nonlinearity,
- (f) Frequency content of reference motion.

The signifcance of valley shape was extensively explored by Bard and Bouchon ([1980a](#page-36-1), [b,](#page-36-2) [1985\)](#page-36-3), who defned the shape ratio (H/B) as the ratio between the maximum thickness (H) and the half-width (B) of the valley (Fig. [1](#page-3-0)).

Fig. 1 Geometrical parameters for alluvial valleys with **a** rectangular, **b** trapezoidal, **c** wedge, and **d** sinusoidal shapes

Based on the results of a series of visco-elastic numerical analyses conducted on homogeneous valleys with either a rectangular or sinusoidal shape, Bard and Bouchon [\(1985](#page-36-3)) observed that the two-dimensional resonance frequency, $f_{0,2D}$, surpassing that of the soil column at the centre of the valley, $f_{0,1D}$, increases with the shape ratio, H/B . It is important to note that the existence of a 2D resonance efect and the proportionality of the frequency to the steepness of morphological irregularities have also been demonstrated by various authors for ridges and crests (e.g., Paolucci [2002;](#page-38-14) Bray [2007\)](#page-37-6), as well as for triangular-shaped embankments or dams (e.g., Dakoulas and Gazetas [1985](#page-37-7)). Bard and Bouchon ([1985\)](#page-36-3) provided the following relationships between the shape ratio and the resonant frequencies for the diferent types of waves:

$$
f_{0,2D}^P = f_{0,1D}^P \cdot \sqrt{1 + \left(\frac{H}{B}\right)^2}
$$

\n
$$
f_{0,2D}^{SV} = f_{0,1D}^{SV} \cdot \sqrt{1 + \left(2.9 \cdot \frac{H}{B}\right)^2}
$$

\n
$$
f_{0,2D}^{SH} = f_{0,1D}^{SH} \cdot \sqrt{1 + \left(2 \cdot \frac{H}{B}\right)^2}
$$
\n(1)

where the superscripts P, SV and SH identify the corresponding compression (P) and shear waves, these latter distinguished between those inducing in-plane (SV) and out-of-plane (SH) motions.

As is well-known, even for one-dimensional propagation, the resonance frequency depends solely on the shape ratio, as well as on the wave velocity and thickness of the

deformable soil. On the other hand, the amplifcation at the surface is proportional to the 'impedance ratio' between the bedrock and the overlying soil, denoted as *I*. This ratio is defned as the ratio between the products of material density and propagation velocity of a given body wave. Its infuence is justifed by the physical refraction phenomenon, wherein seismic waves propagating upward from the bedrock encounter the interface with the alluvial deposit. At this interface, part of the energy is refected downward, while the remaining portion is transmitted toward the basin surface. The refracted energy increases with *I*, while the refected part (and thus, the radiation damping) decreases. Consequently, due to these mechanisms, the amplitude and duration of the surface ground motion generally increase with the impedance contrast. The above mentioned study by Bard and Bouchon ([1985\)](#page-36-3) lead to the definition of a 'critical shape ratio', $(H/B)_{c}$, defined as follows:

$$
\left(\frac{H}{B}\right)_c = \frac{0.65}{\sqrt{C_v - 1}}\tag{2}
$$

i.e. as a function of the ratio, C_V , between the shear wave velocity of the bedrock, V_{SRR} , and that of the overlying soil, V_s . Note that the velocity ratio (C_V) is a parameter less general and slightly lower than *I*, being the density ratio between rocks and soils in alluvial valleys typically variable between 1.15 and 1.50. Valleys characterized by values of C_V and H/B that identify a point below the threshold curve, as shown in Fig. [2,](#page-4-0) can be termed as 'shallow'. In such cases, seismic amplifcation at the surface is primarily due to the combination of stratigraphic one-dimensional resonance and the efect of surface waves. Conversely, if the point falls above the threshold curve, the valley is termed 'deep', and its response is governed by two-dimensional resonance.

The influence of the slope angle α of the edges of a trapezoidal valley was investigated by Zhu and Thambiratnam ([2016\)](#page-39-6), revealing two distinct wave propagation patterns depending on its value. For high angle values (Fig. [3](#page-5-0)a), most of the ray paths of

Fig. 2 Threshold curve of the critical shape ratio vs. the velocity contrast (modifed from Bard and Bouchon [1985](#page-36-3))

Fig. 3 Ray paths in case of **a** high and **b** low inclination of the edge (modifed from Zhu and Thambiratnam [2016\)](#page-39-6)

body waves transmitted from the edges (indicated by red arrows) are directed towards the centre of the valley, where they signifcantly interact with the direct waves (shown by blue arrows). Conversely, for low slope inclinations (Fig. [3b](#page-5-0)), a non-negligible amount of energy becomes trapped within the edges (depicted by green arrows), leading to a substantial amplifcation of motion at the borders of the valley.

Typically, alluvial deposits exhibit non-homogeneity due to a shear wave velocity profle that varies with depth (d''Onofrio and Silvestri [2001\)](#page-37-8), infuencing the seismic response of the valley at the ground surface. A nonlinear increase in the shear wave velocity profle (*Vs*) results in amplifed seismic motion compared to the homogeneous case, both at the edges and the centre of the valley (Bard and Gariel [1986](#page-36-7)). Additionally, at the valley's side, the interface between bedrock and the deformable deposit features a decreasing impedance ratio with depth, impacting the ray paths of both refracted and surface seismic waves. This, in turn, infuences the position of the maximum amplifcation, dependent on the constructive interference between various waves, shifting it towards the valley edge (Bard and Gariel [1986\)](#page-36-7).

Soil non-linearity further modifes the seismic response of the basin, as emphasized in numerous numerical literature studies (e.g., Psarropoulos et al. [2007;](#page-38-15) Gelagoti et al. [2010,](#page-37-9) [2012;](#page-37-10) Iyisan and Khanbabazadeh [2013;](#page-37-11) Riga et al. [2018](#page-38-16); Garini et al. [2020\)](#page-37-12). In one-dimensional propagation of shear waves, the strain-dependent increase in soil deformability and energy dissipation induces signifcant changes along the valley in terms of amplitude, frequency content, and duration of ground motion at the surface. These changes depend on the coupling between soil non-linearity and the characteristics of the reference input motion. Non-linearity often signifcantly afects the surface ground motion along the valley edges, particularly evident when using true nonlinear analyses with hysteretic-perfectly plastic soil models, rather than the more traditional equivalent linear approaches (see, for instance, Capatti et al. [2017\)](#page-37-13).

The seismic response of alluvial valleys is also infuenced by the frequency content of the incoming motion, specifcally by the ratio between the mean frequency of the reference bedrock motion (f_m) and the resonant frequency of the valley, proportional to $f_{0,1D}$. This ratio is inversely proportional to that between the wavelength ($\lambda = V_s/f_m$) and the valley thickness, *H*. If f_m is much lower than $f_{0,1D}$, the amplification is negligible because λ is much greater than *H*, and seismic waves do not interact with the deformable layer. If f_m is close to $f_{0,1D}$, the amplification is mainly due to one-dimensional resonance. Finally, if f_m is greater than $f_{0,1D}$, the amplification is affected by 2D effects, resulting in greater amplifcation than in one-dimensional propagation (Alleanza et al. [2019b](#page-36-8)).

3 The numerical parametric study

An extensive series of seismic response analyses was conducted on homogeneous trapezoidal valleys (see Fig. [1](#page-3-0)b) to assess the impact of geometrical and mechanical parameters on the seismic response at the surface. The geometric characteristics of the models used are summarized in Table [1](#page-6-1); they all share a constant thickness of 100 m and exhibit varying widths to achieve a shape ratio ranging from 0.05 to 0.25. For each H/B value, six diferent edge slopes were considered, ranging from 90° to the value of arctan (H/B), representing a 'wedge' geometry, which consistently corresponds to the minimum inclination.

The mechanical properties utilized in the analyses are outlined in Table [2.](#page-7-0) Both bedrock and alluvial soil were modelled as linear visco-elastic media, with a fxed shear wave velocity of 800 m/s assigned to the bedrock. The shear wave velocity of the soil deposit varied between 100 and 580 m/s. The small-strain damping ratio, D_0 , ranged between 5 and 1% for the soil deposit and was set at 0.5% for the bedrock, resulting inversely proportional to the assigned V_s for each material. The unit weight and Poisson's ratio were kept constant for each material, with values typical for alluvial soils and soft rocks.

Following the criteria established by Bard and Bouchon ([1985\)](#page-36-3), all analyzed models fall into the category of 'shallow valleys,' as depicted by the black dots on the chart in Fig. [4.](#page-8-0)

The resonance frequency reported in Table [2](#page-7-0) is referred to the 1D vertical profle corresponding to the centre of the valley, and it is calculated as:

$$
f_{0,1D} = \frac{V_S}{4H}
$$
 (3)

The 2D numerical simulations were conducted using the fnite diference code FLAC 8.0 (Itasca Consulting Group [2016\)](#page-37-14). The mesh grid consisted of quadrangular elements, with a maximum thickness set as 1/10 of the minimum propagating wavelength, following the Kuhlemeyer and Lysmer [\(1973](#page-38-17)) criterion, considering a maximum frequency of 20 Hz. The analysis domain (Fig. [5](#page-8-1)) was laterally extended for a length equal to one quarter of the width $(b=0.5B)$ $(b=0.5B)$ $(b=0.5B)$, in Fig. 5), while the height of the domain was set to twice the thickness of the valley $(=H, \text{ in Fig. 5}).$ $(=H, \text{ in Fig. 5}).$ $(=H, \text{ in Fig. 5}).$

Free-feld boundary conditions in FLAC were simulated using one-dimensional columns, mimicking the behaviour of a laterally semi-infnite medium, connected to the mesh grid through viscous dashpots. Viscous dampers were placed at the bottom boundary, where the reference input motion was applied as a time history of shear stresses, to simulate a visco-elastic half-space. The viscous material damping was modelled using the Rayleigh formulation. Following the procedure suggested by Costanzo et al. ([2019\)](#page-37-15), the 'single

Thickness H (m)	Width 2B (m)	Shape ratio H/B	Edge slope α $(^\circ)$	Wedge slope (°)
100	4000	0.05	90/60/45/30/15/Wedge	2.86
	2000	0.10		5.71
	1340	0.15		8.53
	1000	0.20		11.31
	800	0.25		14.04

Table 1 Geometrical properties

Fig. 4 Valley schemes considered in the analysis vs. the limit curve defned by Bard and Bouchon [\(1985](#page-36-3))

Fig. 5 Schematic representation of the numerical model

frequency' approach implemented in the numerical code was calibrated to be equivalent to a 'double-frequency' approach. This was achieved by setting the frst reference frequency equal to $f_{0,1D}$ and the second coincident with the predominant frequency of the reference input motion.

For each model, the results of 2D analyses were compared with those obtained from 1D analyses along the soil column corresponding to the centre of the valley. This comparison aimed to isolate geometric efects from stratigraphic ones. The choice of selecting the 1D response at the center of the valley as a reference was preferred to maintain a uniform reference along the valley. Additionally, shallow trapezoidal valleys are characterized by an almost constant thickness, equal to that at the centre, except for a small portion corresponding to the edges.

One-dimensional analyses were performed using the well-known code STRATA (Kottke and Rathje [2008\)](#page-38-18). Given that FLAC and STRATA work in the time and frequency domains, respectively, it was preliminarily checked that, for 1D visco-elastic analysis considering the same subsoil models in terms of boundary conditions and geometric discretization, the two codes provided consistent results, as already shown by previous comparative studies (e.g., Alleanza and Chiaradonna [2018;](#page-36-9) Verrucci et al. [2022\)](#page-39-7).

The infuence of the frequency content of the reference motion was analysed adopting a set of twelve Ricker wavelets as acceleration input motion, a(t), whose analytical expression is:

$$
a(t) = PGA \cdot \left\{ 1 - 2 \cdot \left[\pi \cdot f_m \cdot \left(t - t_0 \right) \right]^2 \right\} \cdot e^{-\left[\pi \cdot f_m \cdot \left(t - t_0 \right) \right]^2} \tag{4}
$$

with a fxed peak ground acceleration amplitude, *PGA*, equal to 0.5 g, a variable mean frequency, f_m , of the Fourier's spectrum, the inverse of which corresponds to half duration of the wavelet and t_0 the time corresponding to the PGA.

The properties of the signals are presented in Table [3](#page-9-0), indicating the ranges of variation for both mean and predominant frequencies (f_n) , corresponding to the peak acceleration of the response spectrum, of the seismic motion in correspondence of outcropping bedrock. The frequency ranges reported in the table are associated with diferent impedance ratio utilized in the study. All models in this investigation share the same valley thickness $(H=100 \text{ m})$, identical bedrock properties $(V_{s,r}=800 \text{ m/s}$ and $\gamma=22 \text{ kN/m}^3$, and 12 values of the ratio λ_m/H , ranging between 20 and 0.5.

Given the latter, the mean frequency of the input was derived for each value of the impedance ratio, and consequently, $f_m = V_s / \lambda_m$. For instance, for wavelet number 1, λ_m / H is equal to 20, thus λ_m is equal to 2000 m. Considering the range of V_s in the parametric analyses between 100 and 580 m/s, the corresponding mean frequencies vary between $100/2000 = 0.05$ Hz and $580/2000 = 0.29$ Hz.

Figure [6a](#page-10-1) displays all the acceleration time histories of the input motions plotted using a normalized time variable $(t \cdot f_m)$, obtained by multiplying the time, *t*, by the mean frequency of the reference input motion. In the normalized plot, accelerograms characterized by different frequency content can be compared since their shape is independent of frequency.

Wavelet #	Mean frequency f_{m} (Hz)	Mean wavelength $\lambda_{\rm m}$ (m)	Predominant Frequency f_{p} (Hz)	$\lambda_{\rm m}$ /H	B/λ_m	$f_{\rm m}$ / $f_{0.1D}$	$T_m/T_{0,1D}$
1	$0.05 - 0.29$	2000.00	$0.06 - 0.37$	20.00	1.00	0.20	5.00
$\overline{2}$	$0.10 - 0.58$	1000.00	$0.13 - 0.74$	10.00	2.00	0.40	2.50
3	$0.11 - 0.64$	900.00	$0.14 - 0.82$	9.00	2.20	0.45	2.25
$\overline{4}$	$0.13 - 0.73$	800.00	$0.17 - 0.93$	8.00	2.50	0.50	2.00
5	$0.14 - 0.83$	700.00	$0.18 - 1.06$	7.00	2.90	0.58	1.75
6	$0.17 - 0.97$	600.00	$0.22 - 1.23$	6.00	3.30	0.67	1.50
7	$0.20 - 1.16$	500.00	$0.26 - 1.49$	5.00	4.00	0.80	1.25
8	$0.25 - 1.45$	400.00	$0.32 - 1.85$	4.00	5.00	1.00	1.00
9	$0.33 - 1.93$	300.00	$0.42 - 2.50$	3.00	6.70	1.30	0.75
10	$0.50 - 2.90$	200.00	$0.64 - 3.70$	2.00	10.00	2.00	0.50
11	$1.00 - 5.80$	100.00	1.28-7.14	1.00	20.00	4.00	0.25
12	$2.00 - 11.60$	50.00	2.56–14.30	0.50	40.00	8.00	0.12

Table 3 Properties of the input motions

Fig. 6 Reference input motions: **a** shape of accelerogram; **b** response spectra; **c** Fourier's spectra

Figure [6](#page-10-1)b and c present the acceleration response spectra and the Fourier spectra of the input motions, respectively. Normalized plots are also used in these cases: the spectral acceleration, $S_a(T)$, in Fig. [6b](#page-10-1) is divided by the peak ground acceleration, PGA, while the amplitudes of each Fourier spectrum are normalized by the relevant maximum value. Additionally, the period and frequency are divided by the respective one-dimensional resonance values, $T_{0,1D}$ and $f_{0,1D}$. The use of wavelets as reference input motions facilitates a detailed analysis of ground motions by identifying direct, indirect, and surface waves, allowing for easier tracking of ray paths within the valley.

A wide frequency range has been investigated, with accelerograms that can be repre-sentative of both impulsive sources (c.f. Fig. [6](#page-10-1)c #9–12) and signals with a wider frequency content (c.f. Fig. $6c$ #1–3).

4 The infuence of diferent factors

By combining 30 geometrical models (5 valley shape factors multiplied by 6 slope angles, as listed in Table [1](#page-6-1)) with 6 shear wave velocity values (as outlined in Table [2](#page-7-0)) and 12 input motions (as detailed in Table [3](#page-9-0)), a total of 2160 two-dimensional analyses were conducted. In contrast, the reference one-dimensional analyses amounted to 72, considering that the soil thickness at the centre of the analyzed models is constant and equal to 100 m.

The results of the parametric analyses were initially presented in terms of time histories of acceleration at the surface, allowing a comparison between the outcomes obtained from 2D and 1D analyses. Furthermore, to emphasize the infuence of subsurface morphology on surface amplifcation, the same results were then synthesized in terms of spectral amplification, A:

$$
A\left(T, \frac{x}{B}\right) = \frac{S_{a,s}\left(T, \frac{x}{B}\right)}{S_{a,r}(T)}
$$
\n⁽⁵⁾

with:

- $S_{a,s}(T, \frac{x}{B})$) : spectral acceleration of ground motion at the surface computed at a distance x from the centre of the valley
- $S_{a,r}(T)$: spectral acceleration of the reference input motion
- $-\frac{x}{B}$ normalized abscissa representing the ratio between the distance from the centre, x, and the half-width of the basin, B,

and fnally, a 'geometrical aggravation factor' was computed as:

$$
AG_{2D/1D}\left(T,\frac{x}{B}\right) = \frac{A_{2D}\left(T,\frac{x}{B}\right)}{A_{1D}(T,0)}
$$
(6)

being A_{2D} and A_{1D} the amplification factors obtained with 2D and 1D analyses, respectively. Note that $AG_{2D/1D}$ is the same aggravation factor as defined by Chávez-García and Faccioli [\(2000](#page-37-4)). Indeed, A_{1D} and A_{2D} are calculated as the ratio of the 1D or 2D spectra at the surface and at the bedrock, and thus $AG_{2D/1D}$ is simply the ratio between the 2D and 1D surface spectra.

In the following, a synthesis of the numerical results is reported with the aim of highlighting the infuence of the single geometrical and mechanical properties on the 2D amplifcation at surface. For each of the analysed factors, some typical and most signifcant results are shown. All the details on the results of the parametric analysis can be found in Alleanza [\(2022](#page-36-10)).

4.1 Infuence of shape ratio

The infuence of the shape ratio, *H*/*B*, on the seismic response can be illustrated through Fig. [7](#page-11-0), which compares the time histories of the horizontal and vertical components of the acceleration at the surface. This comparison is made for two valley schemes characterized by the same impedance ratio ($I=9.26$) and edge slope ($\alpha=45^{\circ}$), but with two different shape ratios: one equal to 0.05 (Fig. $7c-e$ $7c-e$) and the other to 0.25 (Fig. $7d-f$ $7d-f$). The models were subjected to the same input motion #10 (Fig. [7a](#page-11-0)), ensuring that the frequency ratio, $f_m/f_{0.1D}$, was equal to 2 in both cases. The time history of the 1D response at the surface obtained along the profle corresponding to the centre of both valleys is reported in Fig. [7](#page-11-0)b.

Fig. 7 Infuence of shape ratio—Horizontal accelerograms: **a** input motion, **b** computed at the surface of the 1D soil column at the centre of the valley, and along the surface of the valleys with $c H/B = 0.05$ and **d** H/B=0.25. Vertical accelerograms computed along the surface of the valleys with **e** H/B=0.05 and **f** $H/B = 0.25$

The contour plots in this fgure, as well as those in the following, are drawn using a normalized abscissa, x/B , representing the ratio between the distance from the centre, x , and the half-width of the basin, *B*, while the ordinate is the normalized time, as defned in Sect. [2.](#page-2-0)

In the central zone of the flat basin (Fig. [7c](#page-11-0)), the peak motion amplitudes of the horizontal components closely resemble those of the one-dimensional soil column (Fig. [7](#page-11-0)b), aiding in identifying the frst and subsequent arrivals of the upcoming direct and refected shear waves. The interference of body waves with the surface waves generated from the valley edge and propagating within the basin can be clearly identifed by the inclined fringes, forming a sort of 'dromochrone' with a slope approximately equal to the Rayleigh wave velocity. However, in this specific case with the lowest shape ratio ($H/B = 0.05$), they only afect the surface ground motion in a limited zone close to the edges; elsewhere, the horizontal acceleration is similar to that obtained by 1D analysis at the centre of the valley (Fig. [7](#page-11-0)b).

Conversely, for the highest value of the shape ratio, $H/B = 0.25$ (Fig. [7](#page-11-0)d), the seismic motion at the ground surface is signifcantly infuenced by the propagation of Rayleigh waves and their interference with direct and refected waves along the entire basin. The response is diferent from the 1D case everywhere in the valley, including the central zone where the positive peak amplitude is reduced, and a negative peak appears due to the interference. As confrmed by the response of valley models with intermediate values of the shape ratio (Alleanza [2022](#page-36-10)), the value of the peak ground acceleration near the edge is not infuenced by H/B, while its relative position x/B varies, approaching the center of the valley as the shape ratio increases.

On the other hand, if the absolute position is considered, the abscissas of the maximum acceleration are located at the same distance from the edge, confrming the fndings by Zhu and Thambiratnam [\(2016](#page-39-6)), based on the geometry of the interference of wave paths. For edge slopes greater than 30°, the zone of maximum interference between the direct, refected, and refracted waves falls outside that corresponding to the inclined edges and extends for a length equal to $H \cdot \tan(\alpha)$ (Zhu and Thambiratnam [2016\)](#page-39-6). Hence, the zone of the valley afected by the two-dimensional amplifcation phenomena increases with the shape ratio, extending from the edges towards the centre.

These trends are also refected in the vertical accelerations at the surface, which are barely perceptible at the edge of the valley for the lowest H/B (Fig. [7](#page-11-0)e), while they attain a magnitude comparable to the horizontal component at the centre of the valley with $H/B = 0.25$ (Fig. [7f](#page-11-0)). The above results also show that for a high shape ratio, the response is characterized by a marked asynchronism of the seismic motion along the basin, which should be accounted for in the analysis of particularly extensive infrastructures crossing such kinds of valleys, e.g., dams or embankments, pipelines, bridges (see, for instance, Capatti et al. [2017\)](#page-37-13). In the case of very shallow valleys, instead, the motion is in-phase along most of the basin, except for the zone near the edges.

The results of the same analyses are also represented in Fig. [8,](#page-13-0) in terms of the amplifcation function (i.e., the ratio between the Fourier spectra of acceleration at the surface and at bedrock), computed at the ground surface of the 1D profle corresponding to the centre of the valley (Fig. [8](#page-13-0)a), as well as along the basins characterized by $H/B = 0.05$ (Fig. 8b) and $H/B = 0.25$ (Fig. [8](#page-13-0)c). The frequencies are normalized with respect to $f_{0,1D}$, i.e., the fundamental frequency of the 1D profle corresponding to the centre of the valley.

The results confrm what has been already observed in terms of acceleration time histories. In the case of $H/B = 0.05$ (Fig. [8b](#page-13-0)), the amplification function computed within the central part of the valley is very similar to that of the 1D profle (Fig. [8](#page-13-0)a), with the

Fig. 8 Infuence of shape ratio—Amplifcation function for **a** 1D soil column, valleys with **b** H/B=0.05 and **c** H/B=0.25. Acceleration response spectra for: **d** input motion, **e** 1D soil column, valleys with **f** $H/B = 0.05$ and **g** H/B = 0.25. Geometrical aggravation factor $AG_{2D/1D}$ for valleys with **h** $H/B = 0.05$ and **i** $H/B = 0.25$

fundamental frequency equal to $f_{0,1D}$ and a secondary peak at about 3 times this value, while towards the edge, the fundamental frequency shows a slight increase. On the other hand, the amplification function of the valley with $H/B = 0.25$ (Fig. [8](#page-13-0)c) is characterized by a 2D resonance frequency, $f_{0,2D}$, equal to 1.1–1.2 $f_{0,1D}$ in the central area and of the order of 1.8–2 $f_{0,1D}$ at the edge.

To evaluate the aggravation factor, $AG_{2D/1D}$, as defined by Eq. [\(6](#page-11-1)), the data have been first synthesized in terms of response spectra. Figure [8](#page-13-0)f and g show the response spectra obtained along the two valleys, while Fig. [8d](#page-13-0) and e respectively report the spectral acceleration of the input motion and at the surface of the 1D reference profle at the valley centre. The periods are normalized with respect to the resonance period of the reference soil column, $T_{0,1D}$. The spectral amplitudes are represented up to $T/T_{0,1D} = 1$, because for higher values, no signifcant 2D amplifcation efects have been observed, as discussed in detail in the follow. (see also Vessia et al. [2011](#page-39-1)).

In accordance with the previous observations, the spectral response of the valley with $H/B = 0.05$ (Fig. [8f](#page-13-0)) is close to that of the 1D column all along the valley, except for the edge zone. The maximum spectral accelerations correspond to a period next to the predominant period of the input motion (Fig. [8d](#page-13-0)), both at the centre and at the edge of the valley. A further peak amplifcation at higher periods can be detected at the edge of the valley $(x/B = 0.90 - 0.95)$ due to Rayleigh waves.

On the other hand, for the basin characterized by $H/B = 0.25$ (Fig. [8](#page-13-0)g), a marked spatial variability of the spectral response can be observed. At the centre of the valley, the maximum amplification occurs both close to the predominant period ($T/T_{0,1D} = 0.35$) and for longer periods $(T/T_{0.1D} = 0.6 - 0.7)$, probably due to the 2D resonance of the valley.

The previous results are represented in terms of aggravation factor in Fig. [8h](#page-13-0) and i, respectively for the two shape ratios selected. In agreement with what was observed above, for $H/B = 0.05$, the aggravation factor is almost unitary in the central zone and moderately increases towards the edge due to 2D effects (Fig. [8h](#page-13-0)). For $H/B = 0.25$, instead, $AG_{2D/1D}$ is significantly greater than unity in both the central and the lateral zones (Fig. [8](#page-13-0)i), confrming that for high shape ratios (although still lower than the critical value defned by Eq. [1](#page-3-1)) even the surface amplifcation of a so-called 'shallow valley' is substantially influenced by 2D effects.

The choice of considering only the periods lower than $T_{0.1D}$, has been borrowed from previous literature results e.g. Vessia et al. ([2011](#page-39-1)) and Papadimitriou et al. ([2018](#page-38-19)). It is further justified by the results of the numerical analyses shown in Figs. [9,](#page-14-0) [10](#page-15-0) and [11](#page-16-0), where the response spectra computed by 2D analyses at three representative normalised abscissae (x/B = 0, x/B = 0.5, x/B = 0.95) along the very shallow (H/B = 0.05) and shallow valley $(H/B = 0.25)$, are compared to those evaluated at the centre of the valley by 1D analysis and to that of the input motion. In the same fgures the amplifcation factors AG_{1D} and AG_{2D} , as well as their ratio, $AG_{2D/1D}$, are also reported.

As already observed, in the case of the very shallow valley $(H/B = 0.05)$ 2D effects become significant at the edge of the valley. For this reason, the ratio $AG_{2D/1D}$ is equal to unity both at the centre (Fig. [9](#page-14-0)a, c) and at $x/B = 0.5$ (Fig. [10a](#page-15-0), c), whatever the period

Fig. 9 Comparison between the acceleration response spectra (c, d) , AG and AG_{2D/1D} (a, b) obtained at centre of the valley with 2D (black lines), 1D (green lines) analyses, for $H/B = 0.05$ and 0.25

Fig. 10 Comparison between the acceleration response spectra (c, d) , AG and AG_{2D/1D} (**a**, **b**) obtained at $x/B = 0.5$ with 2D (cyan lines), 1D (green lines) analyses, for $H/B = 0.05$ and 0.25

considered. Near the edge (Fig. [11](#page-16-0)a, c), instead, the 2D spectral acceleration is always lower than that of 1D analyses, thus $AG_{2D/1D}$ is lower than 1.

In the case of $H/B = 0.25$, the 2D spectral acceleration at the centre of the valley (Fig. [9b](#page-14-0), d) is higher than that computed by 1D analysis for periods lower than $T_{0,1D}$, while for longer periods the diference between the two spectra is almost negligible.

Moving from the centre of the valley towards the edge, for $x/B = 0.5$ (Fig. [10b](#page-15-0), d) the spectral response is mainly ruled by the predominant period of the input motion, and the 2D spectral acceleration is greater than that relevant to 1D propagation for periods close to the predominant one (T/T_{0,1D} = 0.4). Moreover, for periods greater than T_{0,1D} the 2D spectral ordinates are slightly lower than the corresponding 1D values, hence $AG_{2D/1D}$ is greater than unity for T/T_{0,1D} < 1. Therefore, the 2D effects influence the spectral response for periods shorter than the 1D resonance period, while they become negligible at longer periods.

Finally, for $x/B = 0.95$ and $H/B = 0.25$ (Fig. [11](#page-16-0)b, d), the 2D response is always smaller than the 1D response.

Finally, as expected, the shape ratio also infuences the value of the 2D resonance frequency calculated at the centre of the valley. Figure [12](#page-16-1) summarizes all the results obtained in this study in terms of ratio $f_{0.2D}/f_{0.1D}$ as a function of *H*/*B*, distinguishing by blue and red symbols the results obtained for trapezoidal and wedge valley shapes, respectively. It is apparent that $f_{0,2D}$ always increases with H/B , significantly, depending on the geometry of the valley. As a matter of fact, the values of $f_{0,2D}$ computed in this

Fig. 11 Comparison between the acceleration response spectra (c, d) , AG and AG_{2D/1D} (a, b) obtained at $x/B = 0.95$ with 2D (magenta lines), 1D (green lines) analysis for $H/B = 0.05$ and 0.25

study for wedge-shaped valleys are almost similar to those obtained by Bard and Bouchon [\(1985\)](#page-36-3) for sinusoidal valleys (yellow triangles and curve), and they result higher than those calculated for trapezoidal basins, which in turn are in good agreement with those obtained by Bard and Bouchon ([1985](#page-36-3)) for rectangular valleys.

4.2 Infuence of impedance ratio

The role of impedance ratio on two-dimensional seismic amplifcation at the surface was investigated by assigning fve diferent shear velocity values (listed in Table [2\)](#page-7-0) to the homogeneous soil deposit laying on bedrock characterized by a constant shear wave velocity of 800 m/s. Hereafter, the response obtained applying the same input motion to valleys characterized by the same geometrical shape (H/B = 0.25, α = 45°) and by two different impedance ratios $(I = 1.60$ and 9.26) is compared as a reference example. Figure [13](#page-17-0) shows the horizontal and vertical acceleration computed for both valleys. As expected, the amplifcation and the duration of seismic motion are strongly infuenced by the impedance ratio: the energy transmitted at the edge interface and the amplitude of the generated Rayleigh waves increase with the impedance ratio. In the case of stiff alluvial soil $(I=1.6)$, the horizontal acceleration is poorly amplified (Fig. [13](#page-17-0)b, c), and the vertical accelerations are negligible (Fig. [13g](#page-17-0)) along the whole valley. Instead, in the case of the valley flled with soft soil $(I=9.26)$, 2D amplification and significant vertical motion can be clearly detected (Fig. [13f](#page-17-0), h), as already observed in the previous subsection (see Fig. [7c](#page-11-0), d).

The amplifcation functions along the valley characterized by a low impedance ratio (Fig. [14](#page-18-0)a, b) are almost constant and do not show any signifcant peaks. Thus, the 2D efects are negligible for most of the valley, notwithstanding the relatively high shape ratio equal to 0.25. These trends are confrmed by the 2D spectral accelerations (Fig. [14](#page-18-0)g) that are comparable to those of the 1D column (Fig. [14f](#page-18-0)); both are poorly afected by the propagation, as observed by comparing the results reported in Fig. [14](#page-18-0)e, f, and g. Therefore, the aggravation factor, $AG_{2D/1D}$ (Fig. [14](#page-18-0)m), is almost equal to 1 throughout the entire valley, and thus no appreciable 2D efects can be detected in the case of a low impedance ratio, whereas they are significant for the more deformable basin, as discussed previously (§4.1). This confrms that the seismic response of alluvial valleys is governed by the combination of shape and impedance ratios, rather than by the values assumed by a single parameter (Bard and Bouchon [1980a,](#page-36-1)[b,](#page-36-2) [1985](#page-36-3)).

Fig. 13 Infuence of impedance ratio—Horizontal accelerograms: **a**, **d** input motion, **b**, **e** computed at the surface of the 1D column at the centre of the valley, and along the surface of the valleys with $c = 1.60$ and **f** I=9.26. Vertical accelerograms computed along the surface of the valleys with **g** I=1.60 and **h** I=9.26

Fig. 14 Infuence of impedance ratio—Ratio between Fourier spectra at the surface and the bedrock computed by **a**, **c** 1D analysis at the centre of the valley, **b**, **d** 2D analyses along the valley profle. Acceleration response spectra: **e**, **h** input motion; **f**, **i** computed by 1D analysis at the surface of the column at the centre of the valley; **g**, **l** computed by 2D analyses along the valley surface. Aggravation factor, AG_{2D/1D}, for **m** $I=1.60$ and **n** $I=9.26$

4.3 Infuence of the edge slope

To assess the impact of the edge slope, six diferent angles were considered in the analyses, ranging from 90° to the value corresponding to the wedge shape (i.e., arctan H/B). To better illustrate this efect, the behaviour of two valleys with the same mechanical properties and shape ratio, but with edge slopes (α) of 90° and 45°, respectively, will be compared. The 2D horizontal accelerations computed for both slope angles (Fig. [15c](#page-19-0), d) at the valley centre are comparable to those computed by the 1D analysis (Fig. [15](#page-19-0)b), indicating that the response in the middle of the valley is not signifcantly afected by the edge slope.

A diferent behaviour can be observed at the edge, where the abscissa of the maximum acceleration shifts towards the centre as the slope angle decreases. This is highlighted in Fig. [15](#page-19-0)a and b, where the red arrows indicate the positions of the maximum accelerations, as seen in the case of $\alpha = 90^\circ$ where $x/B = 0.55$, while in the other case $x/B = 0.45$. The time history of the vertical component of the acceleration for a given impedance ratio, I (Fig. [15e](#page-19-0), f), shows that the direction of transmitted waves, and consequently, the location of maximum interaction between the direct and the Rayleigh waves, depends on the slope angle. The maximum accelerations occur at $x/B = 0.85$ for α = 90° and at x/B = 0.75 in the other case.

The amplifcation functions (Fig. [16b](#page-19-1), c) reveal that the slope angle infuences the peak at the frst resonance frequency less signifcantly than those relevant to the higher modes. This effect is confirmed by the response spectra, which for $\alpha = 90^{\circ}$ appear

Fig. 15 Infuence of slope edge—Horizontal accelerograms: **a** input motion; computed at the surface for **b** 1D response at the valley centre; 2D analyses for **c** $\alpha = 90^\circ$ and **d** $\alpha = 45^\circ$. Vertical acceleration for **e** $\alpha = 90^\circ$ and $\mathbf{f} \alpha = 45^\circ$

Fig. 16 Infuence of slope edge—Ratio between Fourier spectra at the surface and bedrock for **a** 1D analysis and 2D analyses for **b** $\alpha = 90^\circ$ and **c** $\alpha = 45^\circ$. Acceleration response spectra for: **d** input motion; **e** 1D analysis; 2D analyses for $f \alpha = 90^\circ$ and $g \alpha = 45^\circ$. Aggravation factor, AG_{2D/1D}, for **h** $\alpha = 90^\circ$ and **i** $\alpha = 45^\circ$

slightly higher both at the centre and towards the edge (Fig. $16f-g$ $16f-g$). This influence is reflected even more apparent by the aggravation factor (Fig. [16h](#page-19-1), i).

4.4 Infuence of frequency of the input motion

To emphasize the efect of the frequency content of the incoming motion, three diferent cases will be examined hereafter, with f_m significantly lower, close to, and higher than $f_{0,1D}$, respectively.

In the case of $f_m/f_{0,1D} = 0.2$ (i.e., $f_m < f_{0,1D}$), which corresponds to $\lambda_m/H = 20$ (i.e., λ > > H), regardless of the valley shape and the impedance ratio (i.e., H/B, I, α), the motion along the surface is not infuenced by the presence of the soil. In other words, the accelerations (Fig. [17b](#page-20-0), c) and the spectra (Fig. [17](#page-20-0)e, f) obtained with 1D and 2D analyses are equal to those of the input motion (Fig. [17](#page-20-0)a, d). This is further confrmed by the absence of any parasitic vertical motion (Fig. [17](#page-20-0)g) and by the aggravation factor $AG_{2D/1D}$ (Fig. 17h), which is equal to unity throughout the entire basin and for all periods.

The surface motion along the valley becomes comparable to the 1D response as the frequency f_m increases, approaching $f_{0,1D}$. Figure [18](#page-21-0) depicts the AG_{2D/1D} calculated for H/B = 0.05 (left plots) and 0.25 (right plots) as the mean frequency varies up to $f_{0,1D}$. For $f_{m}/$ $f_{0,1D}$ =0.58 (Fig. [18a](#page-21-0), b), regardless of the valley shape, the 2D amplification is not significantly diferent from the 1D response. As the frequency increases, for the shallowest valley (H/B = 0.05), the aggravation factor $AG_{2D/1D}$ is at most equal to 1.1 for $f_m = f_{0,1D}$ (Fig. [18](#page-21-0)c, e, g). Conversely, for $H/B = 0.25$, a two-dimensional amplification can be observed already for $f_m/f_{0,1D}$ = 0.67 (Fig. [18d](#page-21-0)), and for f_m close to $f_{0,1D}$ (Fig. [18f](#page-21-0), h), AG_{2D/1D} is at most equal to 1.6–1.7. However, results related to lower impedance ratios, e.g., *I*=3.43, indicate that even for H/B = 0.25, the aggravation factor $AG_{2D/1D}$ is at most 1.1–1.2 for $f_m = f_{0,1D}$ (Alleanza [2022](#page-36-10)). This is because, for high impedance contrast, the shape ratio $H/B = 0.25$ is close to the critical value defned by Bard and Bouchon [\(1985\)](#page-36-3), which identifes the transition from 'shallow' to

Fig. 17 Infuence of the frequency of the input motion—Horizontal accelerograms for **a** input motion and at the surface for **b** 1D analysis, **c** 2D analysis and **g** vertical acceleration for $f_m/f_{0.1D} = 0.2$. Acceleration response spectra for **d** Input motion; **e** 1D analysis; **f** 2D analysis **h** AG_{2D/1D} for $f_m/f_{0,1D} = 0.2$

Fig. 18 Influence of the frequency of–the input motion—AG_{2D/1D} for I=9.26, H/B=0.05 and $f_m/f_{0,1D}$ equal to **a** 0.58, **c** 0.67, **e** 0.80, **g** 1.00. AG_{2D/1D} for I=9.26, H/B=0.25 and $f_m/f_{0.1D}$ equal to **b** 0.58, **d** 0.67, **f** 0.80, **h** 1.00

'deep' valleys. Therefore, in this case, a 2D resonance mechanism is likely to occur, characterized by higher amplifcation in the centre of the valley compared to the edges (Bard and Bouchon [1985\)](#page-36-3).

Finally, if $f_m > f_{0,1D}$, two-dimensional effects predominate over one-dimensional response, and the aggravation factor $AG_{2D/1D}$ is significantly greater than unity, increasing with f_m , as shown in the previous sections.

To verify the efectiveness of the normalised parameters adopted and the generality and sufficiency of the performed analyses, a further set of analyses was carried out considering a reduced valley thickness, H, of 30 m keeping the shape ratio equal to 0.25. All the domain dimensions have been consequently adjusted to guarantee the optimization of the numerical model. The analyses were carried out modelling the deformable soil as a homogeneous viscoelastic material and adopting a reference input motion that ensured a value of frequency ratio, $f_m/f_{0.1D}$, equal to that adopted in the previous set of numerical analyses. The results obtained adopting the reduced geometrical model were then compared to those obtained in the previous set of analyses in terms of $AG_{2D/IP}$.

As an example, the contours of $AG_{2D/1D}$, computed for both thicknesses and for $f_m/f_{0.1D}$ equal to 1 and 2 are plotted in Fig. [19a](#page-22-1)–d, respectively. They show that the model response is independent of the individual values of H, B, x and f_m , if the dimensionless variables H/B, f_m / $f_{0.1D}$ and x/B are the same, thus confirming the validity of the dimensionless variables adopted in the parametric analyses.

Fig. 19 AG_{2D/ID} obtained for: **a** H = 100 m, $f_m/f_{0,1D} = 1$; **b** H = 30 m, $f_m/f_{0,1D} = 1$; **c** H = 100 m, $f_m/f_{0,1D} = 2$; **d** $H = 30$ m, $f_m/f_{0,1D} = 2$

5 Valley amplifcation factor

The above parametric analysis on shallow valley models showed that the two-dimensional amplifcation results signifcant along most part of the alluvial soil surface, thus a valley amplifcation factor was defned with the aim to describe the variability of the aggravation along the valley, as a function of its geometry and mechanical properties.

For each period *T*, the mean value of $AG_{2D/1D}$ obtained from the analyses carried out adopting 12 input motions was calculated at each position *x* along the valley surface, thus obtaining an amplifcation factor independent of the input frequency, as follows:

$$
\overline{AG}_{2D/1D}\left(T,\frac{x}{B}\right) = \frac{1}{12}\sum_{i=1}^{12} AG_{2D/1D}\left(T_i,\frac{x}{B}\right) \tag{7}
$$

The factors thus obtained were further averaged within a period range between 0 s and $T_{0,1D}$ (i.e. the resonance period of 1D soil column at the centre of the valley) and a synthetic *VAF* was then defned as follows:

$$
VAF\left(\frac{x}{B}\right) = \frac{1}{T_{0,1D}} \int_0^{T_{0,1D}} \overline{AG}_{2D/1D}\left(T, \frac{x}{B}\right) \cdot dT \tag{8}
$$

The integral is calculated up to $T_{0,1D}$ because, in this range of periods the ground response seems to be more sensible to 2D effects, as shown in Figs. [9](#page-14-0), [10](#page-15-0) and [11](#page-16-0) and discussed in detail in Sect. [4.1,](#page-11-2) where the spectral accelerations computed by 2D analyses at diferent normalised abscissae (x/B) are compared with the 1D response.

In such a way, the variation of *VAF* along the valley can be viewed as dependent on the shape ratio, the edges slope and the impedance ratio.

In the following elaborations, only VAF values greater than or equal to unity were considered, assuming that the seismic motion at the valley surface is at least equal to that of a 1D column at the centre of the valley. This assumption makes the proposed VAF a conservative design tool, since it does not account for the attenuation that can be generated near to the edges*.* Figure [20](#page-23-0)a–c respectively show the infuence of *H/B*, α and *I* on *VAF*, by taking as reference case the valley model with $H/B = 0.25$, $\alpha = 45^{\circ}$ and *I*=9.26. As shown in Fig. [20b](#page-23-0), the *VAF* of the wedge is everywhere greater than that of any trapezoidal valley, due to the specifc shape that generates peculiar wave interference phenomena. Therefore, in the following only the cases of the trapezoidal basins with α greater than 2 times the wedge slope angle will be considered. Also, the results obtained for $\alpha = 15^{\circ}$ will not be discussed, because for $H/B = 0.20-0.25$ this edge slope is very close to that corresponding to the wedge shape, respectively equal to 11° and 14°.

The three plots show that in the central area the *VAF* increases with *H/B* and *I* and it is independent of α (except for the wedge-shaped valleys). The maximum amplification at the edge is independent of H/B and increases with α and *I*. Its position is strongly infuenced by all the analysed factors, in particular it moves toward the centre as *H/B* and *I* increase and α decreases.

The so called 'shallow valleys' $(H/B < 0.25)$ can be further distinguished into two classes based on the value of the shape ratio. If $H/B < 0.1$ they can be considered as "very shallow" basins with slight aggravation along the central sector (i.e. *VAF* lower than $1.05-1.10$, depending on *I*) and gradually increasing approaching the edges. Instead, if H/B is greater than 0.1 but lower than the critical shape ratio (H/B) _c defined by Bard and Bouchon ([1985](#page-36-3)) (see Eq. ([2\)](#page-4-1)), the distribution of *VAF* along the basin is characterised by two distinct peaks, one corresponding to the centre and a second one near the edges, and the valley can be classifed as "moderately shallow". Table [4](#page-24-0) summarises the infuence of the diferent factors examined on the two-dimensional amplifcation along the valley.

Fig. 20 VAF obtained for variable **a** H/B; **b** α; **c** I

Table 4 Summary of the results	Parameter		Amplification		
		Centre	Edge	tion of edge peak	
	H/B (\uparrow +)	$(† +)$	$(=)$	$(\rightarrow\leftarrow)$	
	α († +)	$(=)$	$(† +)$	(\leftrightarrow)	
	$I(f+)$	$(† +)$	$(† +)$	$(\rightarrow\leftarrow)$	

Key (\uparrow +)=increase; (=)=no influence; (\rightarrow \leftarrow)=moves from edge to centre; (\leftrightarrow) =moves from centre to edge

Based on the observed trends, an analytical formulation of the *VAF* as function of the above-mentioned parameters was fnally obtained.

The variation of *VAF* along the valley was approximated as the sum of two Gaussian-like functions (Fig. [21](#page-24-1)), a first one describing the amplification at the valley centre (blue curve in Fig. [21\)](#page-24-1) and another one expressing its trend along the edges (red curve in Fig. [21](#page-24-1)).

The functional form proposed for analytical predictions of the *VAF* was then defned as follows:

$$
VAF = 1 + (VAF(0) - 1) \cdot f_1\left(\frac{x}{B}, \frac{H}{B}, I\right) + f_2\left(\frac{x}{B}, \frac{H}{B}, I, \alpha\right)
$$
(9)

where *VAF(0)* is the amplification computed at the middle of the valley, f_1 and f_2 the functions describing the *VAF* distributions across the central sector and along the edge, respectively. They can be expressed as:

$$
VAF(0) = 1 + c_0 \cdot \left(1 - \exp\left(-\frac{(I-1)^2}{2 \cdot a_0^2}\right)\right)
$$
 (10)

$$
f_1\left(\frac{x}{B}, \frac{H}{B}, I\right) = \exp\left(-\frac{\left(\frac{x}{B}\right)^2}{2 \cdot a_1^2}\right) \tag{11}
$$

Fig. 21 VAF model proposed in this study

$$
f_2\left(\frac{x}{B}, \frac{H}{B}, I, \alpha\right) = c_2 \cdot \exp\left(\frac{\frac{x}{B} - b_2}{a_2} - \exp\left(\frac{\frac{x}{B} - b_2}{a_2}\right)\right)
$$
(12)

where c_0 , a_0 , a_1 , a_2 , b_2 and c_2 are coefficients defining the Gaussian-like functions. The coefficients were preliminarily obtained by fitting the results of the numerical analyses, then their dependency on the geometrical and mechanical properties of the valley was analytically expressed. The analytical formulations of the coefficients are reported in the Appendix and in Alleanza [\(2022](#page-36-10)).

The five charts in Fig. [22](#page-25-0) show the dependency of the above-described coefficients on the impedance ratio, *I*, and the shape ratio, *H/B*; in the charts, both the data points and the ftting functions are reported with symbols and curves of the same colours.

Rather than reporting a_0 and c_0 , which only depend on H/B (see Eqs. [A.5–](#page-34-0)[A.6\)](#page-34-1), the aggravation factor at the valley centre, $VAF(0)$, is directly represented in Fig. [22](#page-25-0)a as an exponential function of *I*, increasing with H/B and independent of α . For a fixed geometry, *VAF(0)* increases with *I* up to a limit value of impedance ratio increasing with *H/B*, beyond which *VAF(0)* remains constant.

The coefficient a_1 (Fig. [22](#page-25-0)b) describes the extension of the 2D aggravation sector around the centre of the valley; its value decreases with *H/B* and *I*.

Fig. 22 Data points and ftting functions for: **a** VAF(0); **b** a1; **c** a2; **d** b2; **e** c2

The coefficient a_2 (Fig. [22](#page-25-0)c) is proportional to the extension of the 2D aggravation zone at the valley edge and its dependency on *H/B* and *I* should be analysed in combination with the trend of the coefficient $a₁$. It increases with the impedance ratio for *H/B*<0.15 and decreases in the other cases.

The coefficient b_2 , which describes the location (Fig. [22d](#page-25-0)) of the amplification peak at the edge, depends on *H/B, I* and *α*. The lateral peak of the *VAF* moves from the edge towards the middle of the valley as the impedance ratio increases for a given shape ratio, and as the *H/B* increases for a given impedance ratio.

The coefficient c_2 (Fig. [22](#page-25-0)e) is proportional to the amplitude of the peak of *VAF* at the edge and it is a function of *I* and *α*. As for *VAF(0),* there is a limit value of *I* beyond which this peak value remains constant, but, in this case, the maximum value of *VAF* at the edge depends on the edge slope, α , while it is independent of H/B .

Summarising the above observations, the aggravation at the centre of the valley (expressed by $VAF(0)$ and $a₁$) is not influenced by the slope angle, whereas the maximum amplification at the edge (c_2) depends on the impedance ratio I and α , and its position and extension (b_2 and a_2) along the valley vary with both geometrical and mechanical parameters.

The charts in Fig. [23](#page-26-0) compare the values of *VAF* obtained with numerical analysis (solid lines) with those predicted by the analytical functions (dashed lines): it can be noted that the latter generally overestimate the amplification because the coefficients were calibrated with a slightly over-conservative approach. This is more clearly and extensively shown by the scatter plots in Fig. [24,](#page-27-0) reporting the whole amount of the numerical data relevant to each surface node of the meshes plotted versus the corresponding analytical predictions. To better quantify how the accuracy of the proposed method in predicting the seismic motion on the surface of 2D trapezoidal valley, Fig. [25](#page-27-1) shows the relative error for all the considered models, calculated as:

Fig. 23 Comparison between numerical and predicted VAF for: **a** H/B = 0.05 and H/B = 0.25; **b** α = 45° and α =30°; **c** I=9.26 and I=1.60

Fig. 24 Comparison between numerical and predicted VAF for all models

Fig. 25 Relative error calculated for all models

$$
Error = \frac{VAF_{predicted} - VAF_{observed}}{VAF_{observed}} \tag{13}
$$

In the above expression, $VAF_{predicted}$ is calculated using the proposed Eq. [\(9\)](#page-24-2), while $VAF_{observed}$ is the value obtained by 2D visco-elastic analyses.

In Fig. [25](#page-27-1) the scale of colour represents the abscissa, x/B, while the solid and dashed black lines represent the mean and mean \pm standard deviation relative error, respectively. The results show that the error is on average below 10% for all H/B values; moreover, the accuracy of VAF estimation is higher in the zones where the thickness of the valley is constant (i.e. at the centre) and decreases along the edges. Finally, it can be observed that the predicted VAF is generally conservative with respect to that calculated with the numerical analyses since the coefficients in Eq. (9) (9) (9) were calibrated on purpose to overestimate the prediction.

The efectiveness of the proposed defnition of VAF in terms of normalised parameters, already demonstrated with reference to the shape ratio H/B (see Sect. [4\)](#page-10-0), was also evaluated with reference to the impedance and the frequency ratios, by carrying out additional numerical analyses. Therein, the geometric dimensions of the valley were kept constant $(H=100 \text{ m and } H/B = 0.25)$ while the shear wave velocities of the soil and bedrock were proportionally increased, retaining the same impedance ratio $(I=3.43)$ as in some of the previously analysed cases. In detail, a V_{S_r} value of 1200 m/s was used, which is 50% greater than that considered in the other analyses (800 m/s) and the shear wave velocity of the deformable soil was increased to 405 m/s. The input frequencies were also modifed to obtain the same $f_m/f_{0,1D}$ used in the previous set of analyses.

Figure [26](#page-28-1) shows the results of the numerical analyses in terms of VAF, obtained adopting the two couples of values of V_s and $V_{s,r}$, compared with the VAF predicted with the formulas proposed in this study. The numerical values of VAF are independent of the single velocity values, if I is the same, whereas the predicted VAF slightly overestimates the numerical results, given the conservativeness of the proposed formulation.

6 Application of the proposed procedure

In this section, simplifed evaluations of the valley amplifcation factor, VAF, will be applied to study the seismic response of two real valleys in Central Italy.

The frst valley (Fig. [27a](#page-29-0)) consists of gravels, covered and locally interbedded by fne-grained lenses, overlying a limestone bedrock (Lemmi et al. [2017](#page-38-20); Brunelli et al. [2019](#page-37-16), [2021](#page-37-17), [2022](#page-37-18)). It is located in the Italian village of Visso, situated in a highly seismically hazardous area that has experienced numerous destructive events over the centuries. The town was signifcantly afected by the seismic sequence that occurred in

Fig. 26 Comparison between the VAF calculated for different V_{S_r} and that proposed in this study

Fig. 27 Comparison of the VAF calculated from numerical analyses and that proposed for the valleys of **a** Visso and **b** Montefranco

Central Italy since 2016, featuring several earthquakes with a moment magnitude, Mw, ranging between 5 and 6.5.

The cover deposits in the valley can be categorized into three layers with V_s (shear wave velocity) increasing with depth. A shallow fne-grained layer with a thickness of 8 m and V_s =200 m/s overlies a 10 m thick coarse-grained layer with V_s =400 m/s, which in turn covers a 22 m succession of coarse and fine soils with a mean V_s =600 m/s. This layer lies on a bedrock characterized by V_s =1300 m/s. The layered soil profle has been horizontally extended to cover the entire valley, as depicted in the sections in Fig. $27a$ $27a$, where the green colour intensity increases with V_s . The interface between the bedrock and the alluvial soils is highlighted with a red line. The valley section (Fig. [27](#page-29-0)a) has a width of about 410 m, while the thickness is 40 m, resulting in a shape ratio H/B equal to 0.1. The impedance ratio, used to calculate the VAF with the proposed equation, is obtained considering a homogeneous visco-elastic model for the alluvial soil with an equivalent shear wave velocity $V_{s,eq}$ defined as:

Earthquake	Date	M_{w}	Epicentral distance (km)	Station	Site class	Component
Cazulas	24/06/1984	4.9	24	Presa de Beznar	A	$N-S$
Bingol	01/05/2003	6.3	14	Bingol	А	$E-W$
Lazio Abruzzo	07/05/1984	5.9	22	Ponte Corvo	A	$N-S$
Campano Lucano	23/11/1980	6.9	25	Auletta	A	$N-S$
Lazio Abruzzo	07/05/1984	5.9	22	Ponte Corvo	A	$E-W$
Friuli	06/05/1976	6.5	23	Tolmezzo	A	$N-S$
Campano Lucano	23/11/1980	6.9	25	Auletta	A	$E-W$
	Mean	6.2	22			

Table 5 Main features of the 7 accelerograms selected for Visso

Table 6 Main features of the 7 accelerograms selected for Montefranco

Earthquake	Date	M_{w}	Epicentral distance (km)	Station	Site class	Component
Bingol	01/05/2003	6.3	14	Bingol	A	$E-W$
Reykjanes Peninsula	19/03/1990	4.7	16	Reykjavik	A	$N-S$
Izmit (aftershock)	13/09/1999	5.8	15	Izmit	A	$N-S$
Lazio Abruzzo (aftershock)	11/05/1984	5.5	14	Pescasseroli	A	$N-S$
South Iceland (aftershock)	21/06/2000	6.4	6	Selfoss	A	$N-S$
South Iceland (aftershock)	21/06/2000	6.4	15	Hella	A	$E-W$
South Iceland	17/06/2000	6.5	5	Selfoss	A	$E-W$
	Mean	5.9	12			

$$
V_{S,eq} = \frac{H}{\sum_{i=1}^{n} \frac{h_i}{V_{S,i}}} \tag{14}
$$

with H the total thickness of the soil deposit at the centre of the valley, h_i and $V_{S,i}$ the height and shear wave velocity of the i-th layer and n the number of the layers. Therefore the V_{S,eq} is equal to 470 m/s and $\gamma = 20$ kN/m³, while for the bedrock V_S = 1300 m/s and $\gamma = 22$ kN/m³, thus the impedance ratio is about 3.

The second valley (Fig. [27b](#page-29-0)), located in Montefranco (Faralli et al. [2018](#page-37-19)), has a maximum thickness of about 110 m and a width of approximately 850 m. It is predominantly flled with fne-grained soil, resulting in a shape ratio of about 0.26. The soil is nearly homogeneous with $V_s = 260$ m/s and $\gamma = 18$ kN/m³, and the bedrock has $V_s = 850$ m/s and $\gamma = 23$ kN/m³, yielding an impedance ratio of 4.2.

For both valleys, 2D visco-elastic dynamic analyses were conducted using FLAC adopting the actual Vs profles of the valleys. In these analyses, seven natural accelerograms were applied, selected to ensure that the mean response spectrum aligns with the reference one prescribed by the Italian national building code at life limit state (SLV) for the respective sites. Tables [5](#page-30-0) and [6](#page-30-1) show the main properties of the selected signals while the Figs. [28a](#page-31-0) and [29](#page-31-1)a show the comparison among the response spectra of the seven selected accelerograms, the average spectrum and the one defned by NTC ([2018](#page-38-21))

Fig. 28 a Comparison among the response spectra of the 7 input selected for Visso, the average spectrum, and the one defned by NTC ([2018\)](#page-38-21); **b** the same spectra plotted as a function of the normalised period

Fig. 29 a Comparison among the response spectra of the 7 input selected for Montefranco, the average spectrum and the one defned by NTC ([2018\)](#page-38-21); **b** the same spectra plotted as a function of the normalised period

for class A for Visso and Montefranco, respectively. In Figs. [28](#page-31-0)b and [29b](#page-31-1), the same spectra are shown but with the periods scaled with respect to $T_{0,1D}$.

The accelerograms computed at the ground surface were processed to calculate the Valley Amplifcation Factor (VAF) for each surface point. It's important to note that the reference 1D vertical is that of the centre valley of each section. Figure [27a](#page-29-0) and b shows the comparison between the VAF calculated with the numerical analyses and that obtained with the equations proposed in this study.

In the case of Visso (Fig. [27](#page-29-0)a), where the valley is very shallow $(H/B=0.1)$, the average VAF of the seven accelerograms is slightly higher than 1 at the centre of the valley. At the edges, it increases to about 1.3. The trend difers on the two sides of the valley because, on the right, the valley is located at the foot of a slope, while on the left, the surface is almost horizontal. The VAF obtained with the proposed equations (red line) is generally close to the mean VAF, except on the left edge where strong geometric efects, not fully captured by the simplifed model, come into play.

In the case of Montefranco (Fig. [27](#page-29-0)b), where the valley is shallow ($H/B = 0.26$), the mean VAF calculated for the seven accelerograms is approximately 1.3 at the centre and 1.1–1.2 at the edges. Similar to the Visso case, the VAF computed with the proposed

Fig. 30 Comparison between spectra calculated at the centre and edge for **a**, **b** Visso and **c**, **d** Montefranco valley with: 2D visco-elastic analyses (green line); 1D visco-elastic analyses at the centre (blue line); 1D amplify with the proposed VAF (red line); Italian National code for soil class A (dashed black line), B (magenta line) and C (black line)

equations (red line) closely aligns with the mean value for most of the valley, generally falling between the minimum and maximum values.

Finally, Fig. [30](#page-32-0) shows a comparison among the mean response spectra calculated by:

- 2D analyses at the centre and at the edge for the Visso (a,b) and Montefranco (c,d) valleys (green lines);
- 1D analyses carried out along the vertical at the centre valley (blue lines);
- amplifying the 1D spectra of the centre valley with the proposed VAF (red lines).

The spectra specifed by the Italian technical standards for soil classes A, B and C (dashed black line, solid black line and pink lines) are also plotted for reference.

The results highlight that, in the centre of both valleys the proposed VAF leads to a better estimate of the 2D amplifcation, while in the zone close to the edges it is less capable of predicting the expected surface seismic motion, because of the signifcant variability of the 1D frequency response in this zone. However, on average, the suggested approach enables to estimate surface spectra closer to those predicted by 2D analyses with respect to that obtained with 1D analysis.

7 Conclusions

This paper presents the outcomes of extensive parametric numerical analyses investigating the seismic response of 2D symmetrical homogeneous alluvial basins. The study aims to investigate the infuence of both geometric and mechanical parameters on amplifcation along the valley. Authors selected some dimensionless parameters to describe both the geometry and the mechanical characteristics of the valleys. The key fndings underscore the predominant role of the shape ratio (H/B). For very shallow valleys (H/B < 0.1), 2D amplifcation occurs near the edges, while the central part is primarily afected by stratigraphic efects. As H/B increases, 2D efects become signifcant across the entire basin, categorizing the valley as "moderately shallow." The aggravation factor exhibits two peaks, one in the valley's middle and another at the edge. The efectiveness of the selected dimensionless parameters and the generality and sufficiency of the performed analyses were also verifed.

The results obtained can be considered as reliable for the so-called 'shallow valleys', i.e. those characterised by $H/B < 0.3$. They are expected to be extended to the 'deep valley' cases, with a specifcally designed parametric study.

The study further synthesizes numerical results to propose an analytical equation for the Valley Amplifcation Factor (VAF). This equation considers shape ratio, edge slope, and impedance ratio, ofering a tool for preliminary estimation of 2D efects in the case of shallow valleys approximated to a trapezoidal shape, without requiring detailed numerical analysis.

It has been conceived to furnish provide a simple, and efective, but yet a conservative estimation. As a matter of fact, the VAF defned in this study is taken as always greater than 1. This simplifed assumption could lead to a non-realistic prediction of the motion at the edge of the valleys, where the destructive interference between refected, refracted and surface waves could result in a de-amplifcation of the ground motion. Therefore, the VAF, as defned in this study, is reasonably suitable for shallow trapezoidal valleys $(H/B < 0.25-0.3)$, homogeneous and visco-elastic, except for the limited zones near the edges. Furthermore, the defnition of a unique VAF value uniformly increasing the spectral ordinates is an efective straightforward practice-oriented simplifed quantifcation of valley efects, but again it leads to a conservative estimation of spectral ordinates at high periods, since valley efects primarily afect the high high-frequency components of the seismic ground motion. Finally, it is worth highlighting that the proposed VAF can be more reliably adopted with reference to low- to medium-amplitude seismic ground motions, for which non-linearity is not strongly mobilised.

Comparison with 2D visco-elastic analysis for two real valleys in Central Italy, representing very shallow and moderately shallow cases, reveals that the proposed VAF closely aligns with average VAF values obtained from natural accelerograms. Notably, the proposed equation captures key aspects, demonstrating its utility in seismic microzonation studies.

The suggested VAF equation could potentially serve as a reference in defining a coefficient for incorporation into national seismic codes of practice and Eurocode 8 ([2004](#page-37-20)). In other words, VAF might express in-depth morphological amplifcation in a similar way as the wellknown topographic amplification factor, often termed as TAF or S_T , as frequently adopted in the above-mentioned standards.

Additionally, it lays the groundwork for future research to refne simplifying assumptions employed in the proposed equation. As a matter of fact, the efects of heterogeneity and nonlinearity that are not included in this study will be object of future research.

Appendix

$$
VAF = 1 + (VAF(0) - 1) \cdot f_1\left(\frac{x}{B}, \frac{H}{B}, I\right) + f_2\left(\frac{x}{B}, \frac{H}{B}, I, \alpha\right)
$$
 (A.1)

$$
f_1\left(\frac{x}{B}, \frac{H}{B}, I\right) = \exp\left(-\frac{\left(\frac{x}{B}\right)^2}{2 \cdot a_1^2}\right) \tag{A.2}
$$

$$
f_2\left(\frac{x}{B}, \frac{H}{B}, I, \alpha\right) = c_2 \cdot \exp\left(\frac{\frac{x}{B} - b_2}{a_2} - \exp\left(\frac{\frac{x}{B} - b_2}{a_2}\right)\right) \tag{A.3}
$$

$$
VAF(0) = 1 + c_0 \cdot \left(1 - \exp\left(-\frac{(I-1)^2}{2 \cdot a_0^2}\right)\right)
$$
 (A.4)

$$
a_0 = \begin{cases} \frac{H}{B} < 0.10\\ 0.10 \le \frac{H}{B} < 0.15 \ 32.838 \cdot \frac{H}{B} - 2.472\\ \frac{H}{B} \ge 0.15 \ 0.153.290 - 5.574 \cdot \frac{H}{B} \end{cases} \tag{A.5}
$$

$$
c_0 = 2.350 \cdot \left(1 - \exp\left(-\frac{\left(\frac{H}{B}\right)^2}{0.282}\right)\right)
$$
 (A.6)

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$$
a_1 = x_1 \cdot \left(\frac{H}{B}\right)^{x_2} + x_3 \tag{A.7}
$$

$$
a_2 = x_4 + \ln(I^{x_5})
$$
 (A.8)

$$
b_2 = x_6 + \ln(I^{-x_7})
$$
 (A.9)

$$
c_2 = x_{12} \cdot \left(1 - \exp\left(-\frac{I^2}{2 \cdot x_{13}^2}\right)\right) \tag{A.10}
$$

$$
x_1 = 0.204 \cdot I^{-0.409} - 0.00998 \tag{A.11}
$$

$$
x_2 = 0.531 \cdot I^{-0.303} - 1.160 \tag{A.12}
$$

$$
x_3 = -4.495 \cdot I^{-0.0372} + 4.103 \tag{A.13}
$$

$$
x_4 = 0.335 \cdot \left(1 - \exp\left(-\frac{\left(\frac{H}{B}\right)^2}{2 \cdot 0.172^2}\right)\right) \tag{A.14}
$$

$$
x_5 = \begin{cases} \forall \frac{H}{B} \le 0.15 \rightarrow -8.567 \cdot \left(\frac{H}{B}\right)^2 + 1.679 \cdot \frac{H}{B} - 0.0327\\ \forall \frac{H}{B} > 0.15 \rightarrow 1.173 \cdot 10^{-9} \cdot \left(\frac{H}{B}\right)^{-9.421} - 0.0414 \end{cases}
$$
(A.15)

$$
x_6 = x_8 + \ln(\alpha^{x_9})
$$
 (A.16)

$$
x_7 = \begin{cases} \forall \frac{H}{B} < 0.10 \rightarrow -0.0042 + 0.764 \cdot \frac{H}{B} \\ \forall \frac{H}{B} \ge 0.10 \rightarrow x_{10} + \ln(\alpha^{x_{11}}) \end{cases}
$$
(A.17)

$$
x_8 = 0.967 - 5.849 \cdot \frac{H}{B} \tag{A.18}
$$

$$
x_9 = 0.0097 + 1.127 \cdot \frac{H}{B} \tag{A.19}
$$

$$
x_{10} = -0.375 \cdot \ln\left(\frac{H}{B}\right) - 0.793\tag{A.20}
$$

$$
x_{11} = 0.088 \cdot \ln\left(\frac{H}{B}\right) + 0.203\tag{A.21}
$$

$$
x_{12} = 0.207 + 0.00919 \cdot \alpha \tag{A.22}
$$

$$
x_{13} = 1.064 + 0.00416 \cdot \alpha \tag{A.23}
$$

Acknowledgements The study is carried out as part of WP16.1 "Seismic response analysis and liquefaction" in the framework of the research programme funded by Italian Civil Protection through the ReLUIS Consortium (DPC-ReLuis 2019-2021).

Funding Open access funding provided by Università degli Studi di Napoli Federico II within the CRUI-CARE Agreement. This work was supported by the research programme funded by Italian Civil Protection through the ReLUIS Consortium (DPC-ReLuis 2019–2021)—WP16 Task 1 "Analisi di risposta locale e liquefazione".

Declarations

Confict of interest The authors declare that they have no known competing fnancial interests or personal relationships that could have appeared to infuence the work reported in this paper.

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